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# **Ridge Regression in Mediation Analysis with an Application**

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# Abstract

This paper came with the aim of knowing the causal mediation analysis and estimation methods in addition to the study data. Mediation is the basis for many fields, where at the present time the use of mediation analysis has become increasingly common in many areas of scientific research as well in other fields such as economic and social as well as medical sciences. Causal mediation analysis is one of the important methods in order to know the mechanism of influence between variables, which has had a large role among researchers in recent times. In order to arrive at a model that leads to accurate estimates, it is necessary to find or search for the method by which the important variables are chosen in order to be included in the model, especially when the study data suffers from the presence of the problem of linearity. Therefore, many methods of estimating the mediation variables have been used, which are the least squares method and Ridge method. In order to apply the estimation methods, a simple random sample of (50) women were drawn to study the factors affecting the number of births (response variable). The study data were analyzed using programming in R language.

Keywords: multi broker form; Indirect effect, direct effect, Least Squares Estimation, ridge regression

انحدار الحرف في تحليل الوساطة مع التطبيق

زكريا يحيى محمد الزبيدي أ. م. د. أحمد نعيم فليح قسم الإحصاء، كلية الإدارة والاقتصاد، جامعة القادسية العراق - 0069 - واسط ahmad.flaih@qu.edu.iq يعلم تعديم العراق - 0069 - الديوانية

الملخص

جاءت هذه الورقة بهدف معرفة طرق تحليل وتقدير الوساطة السببية بالإضافة إلى بيانات الدراسة. الوساطة هي الأساس للعديد من المجالات، حيث أصبح استخدام تحليل الوساطة في الوقت الحاضر شائعًا بشكل متزايد في العديد من مجالات البحث العلمي وكذلك في مجالات

. Vol. 6 Issue 1 2021

أخرى مثل العلوم الاقتصادية والاجتماعية وكذلك العلوم الطبية. يعتبر تحليل الوساطة السببية من الطرق المهمة لمعرفة آلية التأثير بين المتغيرات والتي كان لها دور كبير بين الباحثين في الآونة الأخيرة. من أجل الوصول إلى نموذج يؤدي إلى تقديرات دقيقة، من الضروري إيجاد أو البحث عن الطريقة التي يتم من خلالها اختيار المتغيرات المهمة ليتم تضمينها في النموذج، خاصةً عندما تعاني بيانات الدراسة من وجود مشكلة الخطية. لذلك، تم استخدام العديد من طرق تقدير متغيرات الوساطة، وهي طريقة المربعات الصغرى وطريقة ريدج. لتطبيق طرق التقدير، تم سحب عينة عشوائية بسيطة من (50) امرأة لدراسة العوامل المؤثرة على عدد المواليد (متغير الاستجابة). تم تحليل بيانات الدراسة باستخدام البرمجة بلغة R.

الكلمات الرئيسية: نموذج وسيط متعدد، تأثير غير مباشر، تأثير مباشر، تقدير المربعات الصغري، انحدار الحرف

### **1. Introduction**

Causal inference is currently an important area of research in statistical sciences there are several different researches using causal Inference, including medicine, economics and sociology causal Inference has become versatile in modern research especially in the medical and health fields (Grotta & Bellocco ,2012).

When there is a relationship between two variables, one independent and the other dependent without any causal explanation explaining the relationship between these two variables in this case comes the role of the researcher in reaching the knowledge of the effect and interpretation of this relationship and this requires the use of the method of mediation analysis model. Therefore, this model is of great importance in the interpretation and knowledge of the causes of the relationship between the cause-and-effect variable depending on the knowledge of one or more mediation variables (Wen, 2013).

Mediation needs to have a third variable called the median let it be (M) and the work of this variable transfer the effect from the independent variable (X) to the dependent variable (Y)  $(X \longrightarrow M \longrightarrow Y)$  This is called indirect effect but for the direct effect is the effect of the independent variable (X) direct with dependent variable (Y) (X \longrightarrow Y) (Murtas, 2016).

Also, when proposing several statistical methods or methods to estimate unknown statistical model parameters if a number of basic assumptions or conditions are met, one of the most famous of these is the least normal squares (OLS) method used to estimate the features of simple and multiple linear regression model due to advantages of this method. It is characterized by the best unbiased linear estimates with the least variation among other unbiased linear estimates. Followed by many researchers who developed different aspects of the problem and methods of solving it, and therefore found ways as possible alternatives to solve this problem gives ease and flexibility in calculations, including the regression of the ridge. So (Hoerl & Kennard, 1970a) added a positive amount between zero and one to the elements of the diameter of the information matrix  $(X^T X)$  to solve this problem, they called that constant the Biasing parameter, and the ridge regression method. Ridge regression is a technology specializing in the analysis of multiple regression data with a multicollinearity problem.

# 2. Linear Regression

A method known as regression concerned with the relationship between variables. The relationship between variables is formulated by functions.

Suppose that the relationship

$$y = B_0 + B_1 x + \epsilon$$

This equation is the simple linear regression model where y is the dependent variable, x is the predictor variable, and  $\epsilon$  is the random error. Whereas,  $B_0$  and  $\beta$  are the regression coefficients.

The multiple linear regression model, in concerned with the relationship between the response variable yi and many predictors,  $xi = (x_{i1}, \dots, x_{ik})$ , for a given n samples,  $(x_i, y_i)_{i=1}^n$ .

The multiple model is

$$yi = \beta_0 + \beta_1 x_{i1} + \beta_2 x_{i2} + \dots + \beta_k x_{ik} + \epsilon_i, \qquad i = 1, 2, \dots, n. \quad (1)$$

The coefficients,  $\beta_0, \beta_1, ..., \beta_k$ , are unknown, and  $\epsilon_1, ..., \epsilon_n$ , are distributed according to  $N(0, \sigma^2)$ .

In a matrix form, the model (2.1) can be written as follows:

$$Y = X\beta + \epsilon, \tag{2}$$

Where

$$Y = \begin{bmatrix} y_1 \\ y_2 \\ \vdots \\ y_n \end{bmatrix}, X = \begin{bmatrix} 1 & x_{11} & x_{12} & \cdots & x_{1k} \\ 1 & x_{21} & x_{22} & \cdots & x_{2k} \\ \vdots & \vdots & \vdots & \ddots & \vdots \\ 1 & x_{n1} & x_{n2} & \cdots & x_{nk} \end{bmatrix}, \beta$$
$$= \begin{bmatrix} \beta_0 \\ \beta_1 \\ \vdots \\ \beta_k \end{bmatrix}, \epsilon = \begin{bmatrix} \epsilon_1 \\ \epsilon_2 \\ \vdots \\ \epsilon_n \end{bmatrix}.$$

So, we have

 $E(\epsilon) = 0$  and  $Cov(\epsilon) = \sigma^2 I_n$ , (3)

Least squares estimation is the well know method to estimates the unknow vector of B.

### 3. Least Squares Estimation

The  $\hat{\beta}$  in LSE is defined by (Montgomery et al. ,2013).

$$\widehat{\beta} = \underset{\beta}{\operatorname{argmin}} RSS(\beta)$$

Where RSS is the residuals sum of squares, i.e.,

$$RSS(\beta) = \sum_{i=1}^{n} (yi - (\beta_0 + \beta_1 x_{i1} + \beta_2 x_{i2} + \dots + \beta_k x_{ik}))^2 \qquad (4)$$

So, the LSE  $(\hat{B})$  is

$$\widehat{\boldsymbol{\beta}} = (\boldsymbol{X}^T \boldsymbol{X})^{-1} \, \boldsymbol{X}^T \boldsymbol{Y}$$

# 4. Collinearity

when the **X** matrix have full rank and the  $(X^T X)$  matrix is nearly singular. The multicollinearity is appear because the columns of **X** correlated so that they are linear dependent. (Gentle, 2007). The effect of multi-collinearity is to make the variances of the parameter estimates inflate.

### 5. Ridge Regression

In recent times, shrinkage techniques are highly accurate and parameter selection is of great importance. The settlement of Tikhonov, a second name for *RR*, deals with many predictors and a matrix of an unconditional form of X (since  $X^TX$  is not reversible or close to singular). Whereas, installing a model with multiple forecasts with no adjustment results in an *LSE* solution. In addition, *LSE* relies on  $(X^TX)^{-1}$  i.e., if the order (X) < k, then  $(X^TX)$  has no inverse. However, *RR* has the potential to overcome these barriers by restricting the coefficient estimates; thus, it Can reduce resident variance and provide some bias, (James, 2013).

RR coefficients are estimated by minimization, similar to LSE:

$$S(\boldsymbol{\beta}, \boldsymbol{\lambda}) = \operatorname{RSS}(\boldsymbol{\beta}) + \boldsymbol{\lambda} \sum_{i=1}^{k} \boldsymbol{\beta}_{i}^{2}$$
 (5)

over  $\beta$  for a given  $\lambda$ , where is called  $\lambda$  a tuning parameter and  $\lambda \ge 0$ . Note the *RSS* ( $\beta$ ) defined in (4). The (*RRE*) ridge regression estimator is denoted by  $\hat{\beta}^{R}(\lambda)$ .

Tikhonov works to find acceptable estimates of the data, by making RSS ( $\beta$ ) small, as well as the term,  $\lambda \sum_{j=1}^{k} \beta_j^2$ , it also becomes small when shrinking estimates ( $\hat{\beta}_1, ..., \hat{\beta}_k$ ) are approximately zero (James et al., 2013). We define (5) in the representation of the vector and vector norm, and their shape will be as follows:

 $\begin{array}{ccc} \min & \|Y - X\beta\|^2 \\ \beta \in \mathbb{R}^k & (6) \\ subject \ to & \|\beta\|_2^2 \le r^2 \end{array}$ 

 $\|\beta\|_2^2 = \sum_{j=1}^k \beta_j^2 \text{ and } r^2 > 0$ , and  $r^2$  be related to  $\lambda$ .

The setting parameter  $\lambda$  plays a very important role here. Controls the relative influence of the two terms in  $S(\beta, \lambda)$ . For example, when the value of  $\lambda = 0$ , it becomes *RR LSE*, but when  $\lambda$  gets bigger,  $\|\hat{\beta}^R\|_2^2$  shrinks; thus, the zero coefficient estimates approach *RR*. And thus, different from *LSE*, for each value  $\lambda$ , we obtain a different set of parameter estimates,  $\hat{\beta}^R(\lambda)$ .

When looking at  $S(\beta, \lambda)$ , we notice that the contraction penalty,  $\lambda \sum_{j=1}^{k} \beta_j^2$ , is applied only to  $\beta_1, \beta_2, ..., \beta_k$  and does not apply to  $\beta_0$ . The term intersection is the measurement of the average value of the response if  $x_{i1} = x_{i2} = \cdots = x_{ik} = 0$ . To delete  $\beta_0$ , we standardize the scales, which means that each column is in the middle so that  $\frac{1}{n} \sum_{i=1}^{n} x_{ij} = 0$  and  $\frac{1}{n} \sum_{i=1}^{k} x_{ij}^2 = 1$ , for j = 1, 2, ..., k. Here we note that standardization occurs if the features in units differ. For convenience, we also focus on outcome values like  $\frac{1}{n} \sum_{i=1}^{k} y_i = 0$ . Once we get the *RR* coefficient estimates, we can retrieve the term intercept by

$$\hat{\beta}_0 = \bar{y} - \sum_{j=1}^k \bar{x}_j \, \hat{\beta}_j^R(\lambda)$$

Where that  $\bar{y}$  and  $\bar{x}_j$ , because j = 1, 2, ..., k, is the original method. Using notation vector and vector norm, we can write an *RR* problem like

 $\begin{array}{ll} \min \ S(\beta,\lambda) &= \min \ \|Y - X\beta\|_2^2 + \lambda \|\beta\|_2^2 \quad for \ som \quad \lambda \ge 0, \\ \beta \in \mathbb{R}^k \qquad \beta \in \mathbb{R}^k \end{array}$ 

Where  $\beta = (\beta_1, \beta_2, ..., \beta_k)$  and  $\|\beta\|_2^2 = \sum_{j=1}^k \beta_j^2$ . Here the matrix X does not include a column of them. This equation (5) is referred to as Lagrangian from *RR*.

We can give another format for the *RR* problem as follows:

$$S(\beta,\lambda) = \sum_{i=1}^{n} (y_i - \sum_{j=1}^{k} x_{ij}\beta_j)^2 + \sum_{i=1}^{k} (0 - \sqrt{\lambda\beta_i})^2$$
(7)

This method reconfigures another *LSE* problem for a set of extended data by adding k views, which results in an expanded sample matrix  $X_{\lambda}$  and  $Y_{\lambda}$  below:

$$X_{\lambda} = \begin{bmatrix} x_{11} & x_{12} & \cdots & x_{1k} \\ x_{21} & x_{22} & \cdots & x_{2k} \\ \vdots & \vdots & \ddots & \vdots \\ x_{n1} & x_{n2} & \cdots & x_{nk} \\ \sqrt{\lambda} & 0 & \cdots & 0 \\ 0 & \sqrt{\lambda} & \cdots & 0 \\ \vdots & \vdots & \ddots & \vdots \\ 0 & 0 & \cdots & \sqrt{\lambda} \end{bmatrix}, \quad Y_{\lambda} = \begin{bmatrix} y_{1} \\ y_{2} \\ \vdots \\ y_{n} \\ 0 \\ 0 \\ \vdots \\ 0 \end{bmatrix}$$

It is clear

Which ultimately results in the solution of RR, (Hoerl and Kennard ,1970),

$$\hat{\beta}^{R}(\lambda) = (X_{\lambda}^{T}X_{\lambda})^{-1}X_{\lambda}^{T}Y_{\lambda} = (X^{T}X + \lambda I_{k})^{-1}X^{T}Y, \quad (8)$$

In the form of LSE.

### 6. Mediation analysis

Most of the research used in many fields focuses on the relationship between two variables, where the independent variable X (cause variable) and the other variable is deliberate variable Y (response) when we add a third variable (M) may be difficult then a new variable called median and be Between the independent variable (X) and the dependent variable (Y) called the mediation variable (M), which explains the effect of the cause variable X on the result variable Y, then the independent variable (X) is the cause of the mediation variable (M), which causes the result variable (Y) ( $X \rightarrow M \rightarrow Y$ ) (D.P.Macimon & Fairchild & Fritz, 2007) (Grotta & Bllocco, 2012).





### 7. Single - Mediator Model

The individual mediation model is one of the simplest models in the analysis of causal mediation. This model consists of three variables X is the independent variable (treatment variable), M mediation variable, Y dependent variable (result variable) so this model is used when the independent variable is changed to This one intermediate variable leads to an effect in the result. This model (Individual Mediator Model), also called individual mediation or simple mediation, has been applied in several areas, including behavioral, social, and educational sciences, which makes the researcher interested to learn about the side effects not studied (wen, 2013).

# 7.1 Regression equations used to evaluate mediation

Baron & Kenny (1986) is one of the most common methods used in the analysis of mediation. This was based on the modeling of linear structural equation (LSEM) in order to provide a mediation approach to an individual median model where the following regression equations are required:

 $Y = r_3 + c'X + bM + e_2$  .....(11)

Whereas:

*Y*: represents the result of interest.

*X*: represents the independent variable (treatment variable).

*M*: Represents the mediation variable.

*C*: represents the relationship between the processing variable and the result in equation (9) where the total effect is called.

C': The parameter that binds as the process variable with the result variable under the influence of the mediation variable is represented in equation (11) where the partial effect is called.

*a*: The parameter that transmits the effect of the processing variable on the mediation variable is in equation (10).

**b**: The parameter that transmits the effect of the mediation variable on the result variable in equation (11).

 $r_1, r_2, r_3$ : objections to each equation.

*e*<sub>1</sub>, *e*<sub>2</sub>, *e*<sub>3</sub>: errors.

**Equation** (9): represents the total effect in Figure (A).

*Equations* (10), (11): Determine the mediation model in Figure (B).

(D.P Mackinnon & pilot, 2015) (Pachali & Mayer & landwehr, 2018)

(Tofighi & Thoemmes, 2014) .



Figure (2) (a) - The direct effects of the X variable on the Y variable.

(b) - Indirect effects of the variable X on the variable Y by the mediation variable M.

The symbols (a, b, c) are considered of particular importance, where (a) denotes the effect of the treatment variable (X) on the mediation variable (M), (b) denotes the effect of the mediation variable (M)on the result variable (Y), (c) denotes the effect of the treatment variable (X) on the outcome variable (Y)(David Mackinnon, 2012) (D.P.Mackinnon, 2007) (D.P.Mackinnon & Pirlott, 2015).

# 8. Multiple Mediator Model

After we describe the individual mediation model, we turn in this part to a broader and more complex mediation model than the previous model, which is a multi-mediation model with a description of its equations with its graphical forms.

# 8.1 Regression equations used to evaluate mediation

In order to provide a mediation approach to the multi-median model, the following regression equation is required:

### whereas

Y: represents the result variable.

X: represents a treatment variable.

 $M_1, \ldots, M_n$ : Causal Mediation Variables.

*C*: The parameter that binds the treatment variable with the outcome variable represents the absence of mediation variables.

C': The parameter that binds the treatment variable to the outcome variable is the effect of the mediation variables.

 $a_1$ : The parameter that associates the transaction variable with the first broker variable.

 $a_n$ : The parameter that links the transaction variable to other mediation variables.

 $b_1$ : The parameter that binds the first mediation variable to the result variable

 $b_n$ : The parameter that links the other mediation variables to the result variable.

 $r_1, r_2, r_3, \dots, r_n$ : are objections in each equation

 $e_1, e_2, e_3, \dots, e_n$ : are errors.

*Equation* (12) is the estimation of the direct effect in the absence of mediation.

*Equations* (13)(14)(15) is the estimation of the indirect effect by the presence of the mediation model (David Mackinnon, 2012).



Figure (3): Represents a diagram of the multi-mediation model using two variables, so the independent variable (X) is related to two arguments  $(M_1)$  and  $(M_n)$  which are related to the dependent variable (Y). Note that there are several other possible mediation models, for example X to  $M_1$  to  $M_n$  to y.

# 9. The Total Effect

The multiple mediation model in Figure (3) consists of two mediation variables whose total effect is the direct effect represented by parameter (C') and the indirect effect of the mediation variables  $(M_1, ..., M_n)$  (Hayes, 2009).

**Total effect** =  $C' + a_1b_1 + \dots + a_nb_n$  ...(16)

# 10. Effect of mediation

We divide the total effect into direct effects, which are represented by the parameter (C') and others that are indirect and that are represented by the effects of the mediator  $(a_1b_1, ..., a_nb_n)$  in the analysis of mediation, so it should be:

$$a_1b_1 + \dots + a_nb_n = C + C' \tag{17}$$

In the case of an unequal reason, this is due to the difference in the sample sizes between the equations Therefore, the parameters of the above models are estimated using different methods, such as (OLS) (Preacher & Hayes, 2008).

# **11.** Testing the importance and confidence intervals of mediation effects

One of the most important methods used to test the significance of the mediation effect (ab) is to estimate the standard error and compare the resulting Z degrees with the critical value of the standard normal distribution (D.P.Mackinnon et al. ,2004).

The standard error and estimated causal mediation effect can also be used to establish

confidence intervals for mediation effect. It is well known that confidence intervals use standard error in estimation, which is why we believe that the confidence intervals used may provide a number of effect values rather than a single value. Therefore, confidence intervals are tools with common uses in research because they ask the researcher to look for the value of the effect as well as its statistical significance (Harlow,nd) and to test the importance of the indirect effect (mediator). So we need to find the standard error of the sample by the median (ab) The most commonly used tests to estimate the standard errors of indirect effect are:

# **11.1** Strategy for causal action to establish mediation for the multi-median model

The multi-mediation form contains a set of steps:

- The treatment variable (X) affects the outcome variable (Y) through (C) as in equation (12).
- 2- The treatment variable (X) affects the mediation of (M<sub>1</sub>, ..., M<sub>n</sub>) by (a<sub>1</sub>) and (a<sub>n</sub>) as in equations (14)(15).
- 3- Mediation variables affect the outcome variables (Y) after controlling the treatment variable (X) factors (b<sub>1</sub>,..., b<sub>n</sub>) as in equation (13).
- 4- The treatment variable must have an unimportant effect (direct effect C') on the outcome variable in order to achieve full mediation as found in equation (5), but if there is an effect of the treatment variable on the outcome variable (C') here is a partial mediation (Wen , 2013).

# 11.2 Product of parameter coefficients testing

The standard error for the internal effect of a multiple mediation model is as follows (David Mackinnon, 2012).

$$S_{a1\ b1} = \sqrt{S_{a1}^2 \ b_1^2 + S_{b1}^2 \ a_1^2} \tag{18}$$

Another variation of the standard error of the multiple mediation model can also be used:

$$S_{a1 b1} + \dots + S_{an bn} = \sqrt{S_{a1}^2 S_{b1}^2 + S_{b1}^2 a_1^2 + \dots + S_{an}^2 b_n^2 + S_{bn}^2 a_n^2 + 2a_1 \dots a_n S_{b1\dots bn}}$$
(19)

Rewrite the equation above as follows:

$$S_{a1\,b1} + \dots + S_{an\,bn} = \sqrt{\frac{S_{a1\,b1}^2 + \dots + S_{an\,bn}^2}{+2a_1, \dots, a_n S_{b1,\dots,bn}}}$$
(20)

 $(2b_1, ..., b_n \ S_{a1,...,an})$  Must be added to the above equations when there is a non-zero difference between  $(a_1, ..., a_n)$ 

 $(S_{b1,\dots,bn})$ : Represents the common difference.

When the overall effect of the medium is present, the standard error is as follows:

### **12. Estimation Methods**

# 12.1 The Method Of Least Squares

This topic will include estimating the expected average of the response variable using the available information from the predictors variables  $(X_1, X_2, ..., X_{19})$  through the use of the three regression models, namely:

*First Model:* Estimating the linear relationship of the regression model (Y/X)

Here the parameters of the predicted variables (X) will be estimated, and the expected mean of the response variable (Y) will be estimated through regression model (12).

Where it will be written as follows:

$$yi = r_1 + \sum_{i=1}^{19} C_i X_i + e_1 \tag{21}$$

where the vector (C) represents the total or direct effect of the predictors variables (X) on the response variable (Y) and the hypothesis test  $H_0: \underline{C} = 0$ , and the table below (1) shows a summary of statistics for the estimated model.

Variable	Estimate	S.E.	t	P-Value
X <sub>1</sub>	1.875	2.363e-01	7.936	7.39e-09 ***
X <sub>2</sub>	-1.562	1.864e-01	-8.379	2.37e-09 ***
X <sub>3</sub>	2.072e-01	1.289e-01	1.607	0.11858
X4	-1.785e-01	1.394e-01	-1.281	0.21008
X <sub>5</sub>	-9.483e-02	1.673e-01	-0.567	0.57502
X <sub>6</sub>	1.013e-01	1.302e-01	0.778	0.44273

Table (1) shows a summary of the estimated model statistics

Vol. 6 Issue 1 2021

Pages 89-111

$X_7$ -1.974e-011.275e-01-1.5480.13200 $X_8$ 2.154e-011.414e-011.5230.13814 $X_9$ 1.841e-011.128e-011.6320.11306 $X_{10}$ 2.941e-011.017e-012.8930.00705 ** $X_{11}$ -1.094e-011.020e-01-1.0730.29198 $X_{12}$ 2.200e-011.058e-012.0780.04634 * $X_{13}$ 1.253e-011.044e-011.2000.23967 $X_{14}$ -3.432e-021.259e-01-0.2730.78699 $X_{15}$ 8.100e-031.150e-010.0700.94432 $X_{16}$ -8.956e-021.187e-01-0.7540.45659 $X_{17}$ 6.112e-021.499e-010.4080.68645					
$X_9$ 1.841e-011.128e-011.6320.11306 $X_{10}$ 2.941e-011.017e-012.8930.00705 ** $X_{11}$ -1.094e-011.020e-01-1.0730.29198 $X_{12}$ 2.200e-011.058e-012.0780.04634 * $X_{13}$ 1.253e-011.044e-011.2000.23967 $X_{14}$ -3.432e-021.259e-01-0.2730.78699 $X_{15}$ 8.100e-031.150e-010.0700.94432 $X_{16}$ -8.956e-021.187e-01-0.7540.45659	<i>X</i> <sub>7</sub>	-1.974e-01	1.275e-01	-1.548	0.13200
$X_{10}$ 2.941e-011.017e-012.8930.00705 ** $X_{11}$ -1.094e-011.020e-01-1.0730.29198 $X_{12}$ 2.200e-011.058e-012.0780.04634 * $X_{13}$ 1.253e-011.044e-011.2000.23967 $X_{14}$ -3.432e-021.259e-01-0.2730.78699 $X_{15}$ 8.100e-031.150e-010.0700.94432 $X_{16}$ -8.956e-021.187e-01-0.7540.45659	X <sub>8</sub>	2.154e-01	1.414e-01	1.523	0.13814
$X_{10}$ $-1.094e-01$ $1.020e-01$ $-1.073$ $0.29198$ $X_{12}$ $2.200e-01$ $1.058e-01$ $2.078$ $0.04634$ * $X_{13}$ $1.253e-01$ $1.044e-01$ $1.200$ $0.23967$ $X_{14}$ $-3.432e-02$ $1.259e-01$ $-0.273$ $0.78699$ $X_{15}$ $8.100e-03$ $1.150e-01$ $0.070$ $0.94432$ $X_{16}$ $-8.956e-02$ $1.187e-01$ $-0.754$ $0.45659$	<i>X</i> 9	1.841e-01	1.128e-01	1.632	0.11306
$X_{11}$ $1.05  0.01$ $1.0200  0.1$ $1.070$ $0.02170$ $X_{12}$ $2.200e-01$ $1.058e-01$ $2.078$ $0.04634  *$ $X_{13}$ $1.253e-01$ $1.044e-01$ $1.200$ $0.23967$ $X_{14}$ $-3.432e-02$ $1.259e-01$ $-0.273$ $0.78699$ $X_{15}$ $8.100e-03$ $1.150e-01$ $0.070$ $0.94432$ $X_{16}$ $-8.956e-02$ $1.187e-01$ $-0.754$ $0.45659$	X <sub>10</sub>	2.941e-01	1.017e-01	2.893	0.00705 **
$X_{12}$ $1.253e-01$ $1.044e-01$ $1.200$ $0.23967$ $X_{14}$ $-3.432e-02$ $1.259e-01$ $-0.273$ $0.78699$ $X_{15}$ $8.100e-03$ $1.150e-01$ $0.070$ $0.94432$ $X_{16}$ $-8.956e-02$ $1.187e-01$ $-0.754$ $0.45659$	X <sub>11</sub>	-1.094e-01	1.020e-01	-1.073	0.29198
$X_{13}$ $-3.432e-02$ $1.259e-01$ $-0.273$ $0.78699$ $X_{15}$ $8.100e-03$ $1.150e-01$ $0.070$ $0.94432$ $X_{16}$ $-8.956e-02$ $1.187e-01$ $-0.754$ $0.45659$	X <sub>12</sub>	2.200e-01	1.058e-01	2.078	0.04634 *
$X_{15}$ 8.100e-03         1.150e-01         0.070         0.94432 $X_{16}$ -8.956e-02         1.187e-01         -0.754         0.45659	X <sub>13</sub>	1.253e-01	1.044e-01	1.200	0.23967
$X_{16}$ -8.956e-02         1.187e-01         -0.754         0.45659	<i>X</i> <sub>14</sub>	-3.432e-02	1.259e-01	-0.273	0.78699
	X <sub>15</sub>	8.100e-03	1.150e-01	0.070	0.94432
X <sub>17</sub> 6.112e-02         1.499e-01         0.408         0.68645	X <sub>16</sub>	-8.956e-02	1.187e-01	-0.754	0.45659
	<i>X</i> <sub>17</sub>	6.112e-02	1.499e-01	0.408	0.68645
$X_{18}$ -5.024e-02 9.762e-02 -0.515 0.61055	X <sub>18</sub>	-5.024e-02	9.762e-02	-0.515	0.61055
X <sub>19</sub> -1.551e-01         1.233e-01         -1.258         0.21816	X <sub>19</sub>	-1.551e-01	1.233e-01	-1.258	0.21816

Table (1) shows the estimated values of the model parameters (12) in addition to the standard errors and the test (t) and the values of (P-Value) where we notice that the variables (Age of the woman) (Woman's age at marriage) (Number of deceased children) (Woman with thyroid disease) have a significant effect level of significance ( $\alpha = 0.05$ ) and this is clear from the values of the column (P-Value) as well as we note from this The table shows that the rest of the variables do not have a significant effect in the study model, and this is clear from the study model, and this is

evident from the values of (P-Value) in comparison with the level of significance ( $\alpha = 0.05$ ).

To test the significance of the estimated model (12) by using the least squares method, we will test the hypothesis.

 $H_0: Ci = 0$  and  $H_1: Ci \neq 0$  i = 1, ..., 19

Where the table below (2) shows the analysis of variance table for the estimated model.

S.O.V	D.F	Sum Sq	Mean Sq	F value	Pr(>F)	R <sup>2</sup>	Adjusted R <sup>2</sup>
Model	19	76.424	4.0223	11.999	2.916e-09***	0.8837	0.8101
Residuals	30	10.056	0.3352	11.777	2.9100 09	0.0057	0.0101
Total	49	86.480					

Table (2) analysis of variance

From the table (2) We note from the value of (Pr(>F)) the significance of the model estimated using the method of least squares, as its value was close to zero and it is less than the level of significance ( $\alpha = 0.05$ ) and thus rejected  $H_0$ .

We also note that the value of  $(R^2)$  is equal to (%88), which is interpreted as the ratio of the total change occurring in the response variable (number of children born) as a result of its effect on the values of the predictors variables (X), where the value of  $(R^2)$  can be considered as an indicator of the suitability of the estimated model or an indicator of the strength of the linear relationship between the number of children born and predictors variables.

We also note the value of  $(Adjusted R^2)$ , which is equal to (%81), which is another measure to judge the extent to which the estimated model matches the data, assuming a change in the number of predictors variables. We can use (*Adjusted*  $R^2$ ) to compare models that have different numbers of predictors variables.

# <u>Second Model:</u> Estimating the Regression Model (Y/X, M)

In this model (13) the parameters of the predictors variables (*X*) will be estimated (C' = partial effect) and the expected estimate of the response variable (*Y*) with another direct estimate called (the mediation effect) by the parameter (*b*) which links the mediation variable to the outcome variable in order to test the partial effect (C'), We will test the following null hypothesis :  $H_0: \underline{C'} =$  0 and  $H_0: b = 0$ , and the table (3) below shows a summary of statistics for the estimated model.

Variable	Estimate	S.E.	t	P-Value
X <sub>1</sub>	1.898	2.343e-01	8.102	1 6.20e-09 ***
X <sub>2</sub>	-1.667	2.015e-01	-8.275	4.01e-09 ***
X <sub>3</sub>	2.279e-01	1.285e-01	1.773	0.0867
X4	-1.859e-01	1.380e-01	-1.347	0.1883
X <sub>5</sub>	-9.658e-02	1.654e-01	-0.584	0.5638
X <sub>6</sub>	1.236e-01	1.299e-01	0.951	0.3493
X <sub>7</sub>	-1.958e-01	1.261e-01	-1.553	0.1312
X <sub>8</sub>	2.511e-01	1.425e-01	1.762	0.0886
X9	2.299e-01	1.170e-01	1.965	0.0590
X <sub>10</sub>	1.603e-01	1.440e-01	1.114	0.2746
X <sub>11</sub>	-1.249e-01	1.016e-01	-1.230	0.2286

Table (3) shows a summary of the estimated model statistics

Vol. 6 Issue 1 2021

Pages 89-111

X <sub>12</sub>	2.175e-01	1.047e-01	2.077	0.0467 *
X <sub>13</sub>	1.410e-01	1.040e-01	1.356	0.1855
X <sub>14</sub>	-7.211e-02	1.278e-01	-0.564	0.5770
X <sub>15</sub>	3.036e-02	1.150e-01	0.264	0.7937
X <sub>16</sub>	-1.037e-01	1.179e-01	-0.879	0.3865
X <sub>17</sub>	4.531e-02	1.488e-01	0.305	0.7629
X <sub>18</sub>	-1.043e-01	1.051e-01	-0.992	0.3293
<i>X</i> <sub>19</sub>	-3.048e-01	1.678e-01	-1.816	0.0797
М	2.439e-01	1.880e-01	1.298	0.2046

Table (3) shows the estimated values of the model parameters (13) in addition to the standard errors and the test (t) and the values of (P-Value) where we notice that the variables (Age of the woman) (Woman's age at marriage) (Woman with thyroid disease) have a significant effect level of significance ( $\alpha = 0.05$ ) and this is clear from the values of the column (P-Value) as well as we note from this The table shows that the rest of the variables do not have a significant effect in the study model, and this is evident from the values of

(P-Value) in comparison with the level of significance ( $\alpha = 0.05$ ).

To test the significance of the estimated model (13) by using the least squares method, we will test the hypothesis.

 $H_0: Ci = 0$  and  $H_1: Ci \neq 0$  i = 1, ..., 19 $H_0: b = 0$  and  $H_1: b \neq 0$ 

Where the table below (4) shows the analysis of variance table for the estimated model.

S.O.V	D.F	Sum Sq	Mean Sq	F value	<b>Pr(&gt;F)</b>	$R^2$	Adjusted R <sup>2</sup>
Model	20	76.976	3.8488	11 744	4 965 - 00 ***	0 2001	0.9142
Residuals	29	9.504	0.3277	11.744	4.865e-09 ***	0.8901	0.8143
Total	49	86.480					

 Table (4) analysis of variance

From the table (4) We note from the value of (Pr(>F)) the significance of the model estimated using the method of least squares, as its value was close to zero and it is less than the level of significance ( $\alpha = 0.05$ ) and thus rejected  $H_0$ .

We also note that the value of  $(R^2)$  is equal to (%89), which is interpreted as the ratio of the total change occurring in the response variable (number of children born) as a result of its effect on the values of the predictors variables (X) by the parameter (b) which links the mediation variable to the outcome variable in order to test the partial

effect (C'), where the value of ( $R^2$ ) can be considered as an indicator of the suitability of the estimated model or an indicator of the strength of the linear relationship between the number of children born and predictors variables.

We also note the value of  $(Adjusted R^2)$ , which is equal to (%81), which is another measure to judge the extent to which the estimated model matches the data, assuming a change in the number of predictors variables. We can use  $(Adjusted R^2)$ to compare models that have different numbers of predictors variables. <u>Third Model</u>: Estimating the Regression Model (M/X)

In this model (14), the effect of the parameters of the predictor's variables (X) on the mediation variable (M) will be estimated in order to test the direct effect (a).

Null hypothesis:  $H_0: a = 0$ 

and the table (5) below shows a summary of statistics for the estimated model.

Variable	Estimate	S.E.	t	P-Value
X <sub>1</sub>	-6.357e-02	1.527e-01	-0.416	0.6801
X <sub>2</sub>	2.917e-01	1.204e-01	2.422	0.0217 *
X <sub>3</sub>	-5.705e-02	8.331e-02	-0.685	0.4987
X4	2.022e-02	9.007e-02	0.224	0.8239
X <sub>5</sub>	4.825e-03	1.081e-01	0.045	0.9647
X <sub>6</sub>	-6.144e-02	8.413e-02	-0.730	0.4709
X <sub>7</sub>	-4.346e-03	8.238e-02	-0.053	0.9583
X <sub>8</sub>	-9.840e-02	9.137e-02	-1.077	0.2901
X9	-1.262e-01	7.288e-02	-1.732	0.0936
X <sub>10</sub>	3.689e-01	6.569e-02	5.616	4.10e-06 ***
X <sub>11</sub>	4.277e-02	6.591e-02	0.649	0.5214
X <sub>12</sub>	6.950e-03	6.840e-02	0.102	0.9197
X <sub>13</sub>	-4.335e-02	6.749e-02	-0.642	0.5256
X <sub>14</sub>	1.042e-01	8.133e-02	1.282	0.2098
X <sub>15</sub>	-6.140e-02	7.432e-02	-0.826	0.4152
X <sub>16</sub>	3.894e-02	7.673e-02	0.507	0.6155
X <sub>17</sub>	4.362e-02	9.689e-02	0.450	0.6558
X <sub>18</sub>	1.492e-01	6.308e-02	2.365	0.0247 *
X <sub>19</sub>	4.128e-01	7.966e-02	5.182	1.39e-05 ***

# Table (5) shows a summary of the estimated model statistics

Table (5) shows the estimated values of the model parameters (14) in addition to the standard errors and the test (t) and the values of (P-Value) where we notice that the variables (Woman's age at marriage) (Number of deceased children) (Match the blood) (Gestational diabetes) have a significant effect level of significance ( $\alpha = 0.05$ ) and this is clear from the values of the column (P-Value) as well as we note from this The table shows that the rest of the variables do not have a significant effect in the study model, and this is

evident from the values of (P-Value) in comparison with the level of significance ( $\alpha = 0.05$ ).

To test the significance of the estimated model (14) by using the least squares method, we will test the hypothesis.

$$H_0: a = 0$$
 and  $H_1: a \neq 0$   $i = 1, ..., 19$ 

Where the table below (6) shows the analysis of variance table for the estimated model.

S.O.V	D.F	Sum Sq	Mean Sq	F value	<b>Pr(&gt;F)</b>	R <sup>2</sup>	Adjusted R <sup>2</sup>
Model	19	17.9813	0.94639	6.762	2.218e-06 ***	0.8107	0.6908
Residuals	30	4.1987	0.13996	0.762	2.2100 00	0.0107	0.0900
Total	49	22.1800					

#### Table (6) analysis of variance

From the table (6) We note from the value of (Pr(>F)) the significance of the model estimated using the method of least squares, as its value was close to zero and it is less than the level of significance ( $\alpha = 0.05$ ) and thus rejected  $H_0$ .

We also note that the value of  $(R^2)$  is equal to (%81), which is interpreted the effect of the parameters of the predictors variables (X) on the mediation variable (M) which will be estimated in order to test the direct effect (a), where the value of  $(R^2)$  can be considered as an indicator of the suitability of the estimated model or an indicator of the strength of the linear relationship between

the number of children born and predictors variables.

We also note the value of ( $Adjusted R^2$ ), which is equal to (%69), which is another measure to judge the extent to which the estimated model matches the data, assuming a change in the number of predictors variables. We can use ( $Adjusted R^2$ ) to compare models that have different numbers of predictors variables.

### 12.2 Ridge Regression Method

Ridge regression provides us with an alternative style or method for estimating, which means that it is an alternative estimation method

for model parameters when we find that the predictors variables have high correlations between them. Depending on the correlations matrix, we find that there are variables that have high correlations between them, which means that there is a problem of linear multiplicity, as the least squares method is known to be ineffective in the presence of the problem of linear multiplicity, so we will resort to the Ridge method in estimating the parameters.

<u>*First Model:*</u> Estimating the linear relationship of the regression model (Y/X)

In this model (21) the parameters of the predictors variables (X) will be estimated and the expected mean of the response variable (Y) will be estimated through regression model (21), as the vector (C) represents the total or direct effect of the predictors variables (X) on the response variable (Y) and the hypothesis test  $H_0: \underline{C} = 0$ , and the table (7) below shows a summary of statistics for the estimated model.

Variable	Estimate	S.E. t		<b>P-Value</b>
<i>X</i> <sub>1</sub>	1.803	3.301e-01	5.461	4.73e-08 ***
<i>X</i> <sub>2</sub>	-1.033	3.823e-01	-2.702	0.00690 **
<i>X</i> <sub>3</sub>	-4.344e-02	4.467e-01	-0.097	0.92253
<i>X</i> <sub>4</sub>	-1.159e-01	4.272e-01	-0.271	0.78614
$X_5$	1.343e-01	3.942e-01	0.341	0.73336
<i>X</i> <sub>6</sub>	-3.874e-01	4.435e-01	-0.874	0.38238
<i>X</i> <sub>7</sub>	-6.236e-01	4.435e-01	-1.406	0.15973
<i>X</i> <sub>8</sub>	1.176	4.154e-01	2.829	0.00466 **
<i>X</i> 9	8.304e-02	4.625e-01	0.180	0.85750
X <sub>10</sub>	1.890	4.726e-01	3.999	6.35e-05 ***
<i>X</i> <sub>11</sub>	5.599e-01	4.686e-01	1.195	0.23214
<i>X</i> <sub>12</sub>	5.370e-01	4.597e-01	1.168	0.24272
<i>X</i> <sub>13</sub>	3.367e-01	4.668e-01	0.721	0.47077
<i>X</i> <sub>14</sub>	6.738e-01	4.460e-01	1.511	0.13088
<i>X</i> <sub>15</sub>	5.078e-02	4.594e-01	0.111	0.91197
<i>X</i> <sub>16</sub>	5.939e-01	4.537e-01	1.309	0.19054
<i>X</i> <sub>17</sub>	-2.063e-01	4.119e-01	-0.501	0.61647
X <sub>18</sub>	-5.759e-01	4.762e-01	-1.209	0.22656
<i>X</i> <sub>19</sub>	6.277e-01	4.569e-01	1.374	0.16953

#### Table (7) shows a summary of the estimated model statistics

Table (7) shows the estimated values of the model parameters (21) in addition to the standard errors and the test (t) and the values of (P-Value) where we notice that the variables (Age of the woman) (Woman's age at marriage) (The age of the husband) (Number of deceased children) have a significant effect level of significance ( $\alpha = 0.05$ )

and this is clear from the values of the column (P-Value) as well as we note from this The table shows that the rest of the variables do not have a significant effect in the study model, and this is evident from the values of (P-Value) in comparison with the level of significance ( $\alpha = 0.05$ ).

To test the significance of the estimated model (21) by using the ridge method, we will test the hypothesis  $H_0: Ci = 0$  and  $H_1: Ci \neq 0$ i = 1, ..., 19 Where the table below (8) shows the analysis of variance table for the estimated model.

S.O.V	D.F	Sum Sq	Mean Sq	F value	<b>Pr</b> (> <b>F</b> )	<b>R</b> <sup>2</sup>	Adjusted R <sup>2</sup>
Model	19	75.23	3.95947	10 5596	1 225024- 02	0.8600	0 7975
Residuals	30	11.25	0.375	10.5586	1.385924e-08	0.8699	0.7875
Total	49	86.48					

#### Table (8) analysis of variance

From the table (8) We note from the value of (Pr(>F)) the significance of the model estimated using the method of ridge, as its value was close to zero and it is less than the level of significance  $(\alpha = 0.05)$  and thus rejected  $H_0$ .

We also note that the value of  $(R^2)$  is equal to (%86), which is interpreted as the ratio of the total change occurring in the response variable (number of children born) as a result of its effect on the values of the predictors variables (X), where the value of  $(R^2)$  can be considered as an indicator of

the suitability of the estimated model or an indicator of the strength of the linear relationship between the number of children born and predictors variables.

We also note the value of (*Adjusted*  $R^2$ ), which is equal to (%78), which is another measure to judge the extent to which the estimated model matches the data, assuming a change in the number of predictors variables. We can use (*Adjusted*  $R^2$ ) to compare models that have different numbers of predictors variables.



Figure (4) a schematic diagram of the first model using the ridge method

<u>Second Model</u>: Estimating the Regression Model (Y/X, M)

In this model (13) the parameters of the predicted variables (X) will be estimated and the

expected estimate of the response variable (Y) with another direct estimate called (the mediation effect) by the parameter (b) which links the mediation variable to the outcome variable in order

to test the partial effect (C'), null hypothesis :  $H_0: \underline{C}' = 0$  and  $H_0: b = 0$  and the table (9) below shows a summary of statistics for the estimated model.

Variable	Estimate	S.E.	t	P-Value
X <sub>1</sub>	1.576	3.024e-01	5.211	1.88e-07 ***
<i>X</i> <sub>2</sub>	-9.304e-01	3.494e-01	-2.663	0.00774 **
<i>X</i> <sub>3</sub>	-3.064e-02	4.162e-01	-0.074	0.94132
<i>X</i> <sub>4</sub>	-7.819e-02	3.977e-01	-0.197	0.84415
<i>X</i> <sub>5</sub>	1.160e-01	3.670e-01	0.316	0.75202
<i>X</i> <sub>6</sub>	-3.143e-01	4.116e-01	-0.763	0.44518
X <sub>7</sub>	-5.773e-01	4.131e-01	-1.397	0.16229
X <sub>8</sub>	1.088	3.841e-01	2.833	0.00461 **
X9	9.107e-02	4.315e-01	0.211	0.83286
<i>X</i> <sub>10</sub>	1.637	4.165e-01	3.930	8.48e-05 ***
X <sub>11</sub>	5.365e-01	4.365e-01	1.229	0.21903
X <sub>12</sub>	4.710e-01	4.269e-01	1.103	0.26992
X <sub>13</sub>	3.137e-01	4.360e-01	0.720	0.47181
X <sub>14</sub>	6.153e-01	4.140e-01	1.486	0.13725
X <sub>15</sub>	6.966e-02	4.265e-01	0.163	0.87025
X <sub>16</sub>	5.856e-01	4.232e-01	1.384	0.16645
X <sub>17</sub>	-2.205e-01	3.820e-01	-0.577	0.56380
X <sub>18</sub>	-5.766e-01	4.425e-01	-1.303	0.19261
X <sub>19</sub>	4.420e-01	3.942e-01	1.121	0.26216
М	6.310e-01	3.621e-01	1.743	0.08138

### Table (9) shows a summary of the estimated model statistics

Table (9) shows the estimated values of the model parameters (13) in addition to the standard errors and the test (t) and the values of (P-Value) where we notice that the variables (Age of the woman) (Woman's age at marriage) (The age of the husband) (Number of deceased children) have a significant effect level of significance ( $\alpha = 0.05$ ) and this is clear from the values of the column (P-

Value) as well as we note from this The table shows that the rest of the variables do not have a significant effect in the study model, and this is evident from the values of (P-Value) in comparison with the level of significance ( $\alpha = 0.05$ ).

To test the significance of the estimated model (13) by using the ridge method, we will test the hypothesis.

$$H_0: Ci = 0$$
 and  $H_1: Ci \neq 0$   $i = 1, ..., 19$ 

 $H_0: b = 0$  and  $H_1: b \neq 0$ 

Where the table below (10) shows the analysis of variance table for the estimated model.

S.O.V	D.F	Sum Sq	Mean Sq	F value	<b>Pr(&gt;F</b> )	<b>R</b> <sup>2</sup>	Adjusted R <sup>2</sup>
Model	20	75.59	3.7795	10.06479	2.01072500	0.9740	0.7972
Residuals	29	10.89	0.3755172	10.06478	3.010735e-08	0.8740	0.7872
Total	49	86.48					

Table (10) analysis of variance

From the table (10) We note from the value of (Pr(>F)) the significance of the model estimated using the method of ridge, as its value was close to zero and it is less than the level of significance ( $\alpha = 0.05$ ) and thus rejected  $H_0$ .

We also note that the value of  $(R^2)$  is equal to (%87), which is interpreted as the ratio of the total change occurring in the response variable (number of children born) as a result of its effect on the values of the predictors variables (X) by the parameter (b) which links the mediation variable to the outcome variable in order to test the partial

effect (C'), where the value of ( $R^2$ ) can be considered as an indicator of the suitability of the estimated model or an indicator of the strength of the linear relationship between the number of children born and predictors variables.

We also note the value of ( $Adjusted R^2$ ), which is equal to (%78), which is another measure to judge the extent to which the estimated model matches the data, assuming a change in the number of predictors variables. We can use ( $Adjusted R^2$ ) to compare models that have different numbers of predictors variables.



Figure (5) a schematic diagram of the second model using the ridge method

<u>Third Model</u>: Estimating the Regression Model (M/X)

In this model (14), the effect of the parameters of the predicted variables (X) on the mediation variable (M) will be estimated in order to test the direct effect (a) Null hypothesis:  $H_0: a = 0$ 

and the table (11) below shows a summary of statistics for the estimated model.

Variable	Estimate	S.E.	t	P-Value	
X <sub>1</sub>	6.250e-01	2.840e-01	2.201	0.02773 *	
X <sub>2</sub>	8.019e-01	3.102e-01	2.585	0.00973 **	
X <sub>3</sub>	-7.287e-02	3.134e-01	-0.233	0.81611	
X4	-1.420e-01	3.135e-01	-0.453	0.65059	
X <sub>5</sub>	1.782e-01	3.077e-01	0.579	0.56244	
X <sub>6</sub>	-3.158e-01	3.156e-01	-1.001	0.31699	
X <sub>7</sub>	7.265e-02	3.161e-01	0.230	0.81819	
X <sub>8</sub>	-2.938e-01	3.266e-01	-0.900	0.36835	
X <sub>9</sub>	-2.692e-01	3.126e-01	-0.861	0.38907	
X <sub>10</sub>	1.731	3.122e-01	5.543	2.98e-08 ***	
X <sub>11</sub>	6.612e-02	3.178e-01	0.208	0.83517	
X <sub>12</sub>	2.022e-01	3.229e-01	0.626	0.53109	
X <sub>13</sub>	-5.785e-02	3.135e-01	-0.185	0.85359	
X <sub>14</sub>	3.416e-01	3.179e-01	1.075	0.28257	
X <sub>15</sub>	-4.555e-01	3.138e-01	-1.451	0.14667	
X <sub>16</sub>	-1.425e-01	3.139e-01	-0.454	0.64996	
X <sub>17</sub>	1.525e-01	3.176e-01	0.480	0.63107	
X <sub>18</sub>	6.039e-01	3.121e-01	1.935	0.05296	
X <sub>19</sub>	1.910	3.112e-01	6.138	8.36e-10 ***	

### Table (11) shows a summary of the estimated model statistics

Table (11) shows the estimated values of the model parameters (14) in addition to the standard errors and the test (t) and the values of (P-Value)

where we notice that the variables (Age of the woman) (Woman's age at marriage) (Number of deceased children) (Gestational diabetes) have a significant effect level of significance ( $\alpha = 0.05$ ) and this is clear from the values of the column (P-Value) as well as we note from this The table shows that the rest of the variables do not have a significant effect in the study model, and this is evident from the values of (P-Value) in comparison with the level of significance ( $\alpha =$ 0.05). To test the significance of the estimated model (14) by using the ridge method, we will test the hypothesis.

 $H_0: a = 0$  and  $H_1: a \neq 0$ , where the table below (12) shows the analysis of variance table for the estimated model.

S.O.V	D.F	Sum Sq	Mean Sq	F value	<b>Pr(&gt;F)</b>	<b>R</b> <sup>2</sup>	Adjusted R <sup>2</sup>
Model	19	6.3	0.3315789	0 (2(409)	0.8557050	0.7150	0.5260
Residuals	30	15.88	0.5293333	0.6264086	0.8557959	0.7159	0.5360
Total	49	22.18					

# Table (12) analysis of variance

From Table (12) we note that the value of (Pr (> F)) is not significant using the Ridge method as its value was not close to zero and it is greater than the level of significance ( $\alpha = 0.05$ ), thus accepting  $H_0$ .

We also note that the value of  $(R^2)$  is equal to (%71), which is interpreted the effect of the parameters of the predictors variables (X) on the mediation variable (M) which will be estimated in order to test the direct effect (a) , where the value of  $(R^2)$  can be considered as an indicator of the

suitability of the estimated model or an indicator of the strength of the linear relationship between the number of children born and predictors variables.

We also note the value of  $(Adjusted R^2)$ , which is equal to (%53), which is another measure to judge the extent to which the estimated model matches the data, assuming a change in the number of predictors variables. We can use  $(Adjusted R^2)$ to compare models that have different numbers of predictors variables.



Figure (6) a schematic diagram of the third model using the ridge method

### 13. Conclusions

- 1- The effectiveness of the ridge regression method, which made the model more interpretable, in addition to choosing the easiest variables.
- 2- The emergence of the insignificance of some variables in the least squares method, the ridge regression method, and the lasso regression method despite its importance due to the presence of the problem of linear multiplicity and this is evident in the lack of significance of the mediation.
- 3- The emergence of some regression coefficients in the least squares method and the ridge regression method with an algebraic sign not identical to the reality of the studied phenomenon This is an indication of the inaccuracy of these methods in constructing a prediction model in the case of a multiplicity problem.

### 14. Recommendations

- 1- We recommend using the ridge regression method for selecting variables because it is able to reduce the parameter estimation to almost zero by imposing a restriction on the sum of the squares of the Rss regression.
- 2- We recommend using the Lasso method when the matrix  $(X^{\wedge'} X)$  suffers from lack of an inverse value or when P> n. The Lasso method provides the best method for selecting the variables Variable Selection and is better than the ridge regression RR.

3- Not relying on the least squares method and the ridge regression method because they do not fully address the problem of linear multiplicity, especially in social studies, or when the number of independent variables is greater.

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